

# (University of Choice) MASINDE MULIRO UNIVERSITY OF SCIENCE AND TECHNOLOGY (MMUST)

#### **MAIN CAMPUS**

### UNIVERSITY EXAMINATIONS 2021/2022 ACADEMIC YEAR

#### SECOND YEAR SECOND SEMESTER EXAMINATIONS

## FOR DIPLOMA IN ELECTRICAL AND ELECTRONICS ENGINEERING

**COURSE CODE:** 

**DEE 071** 

**COURSE TITLE:** 

**ENGINEERING MATHEMATICS IV** 

DATE: Monday 25th April, 2022

TIME: 8.00 AM-10.00AM

#### INSTRUCTIONS TO CANDIDATES

Question ONE (1) is compulsory Answer Any Other TWO (2) questions

TIME: 2 Hours

MMUST observes ZERO tolerance to examination cheating

This Paper Consists of 3 Printed Pages. Please Turn Over.

#### **QUESTION ONE**

- a) Using first principles derivation, show that the Laplace transform of first derivative is given by  $L\{f'(t)\} = sL\{f(t)\} f(0)$  hence show that laplace transform of  $e^{-at} = \frac{1}{s+a}$  (7 Marks)
- b) Using a standard list of laplace transforms, determine the following:

i) 
$$6\sin 3t - 4\cosh 5t$$
 (2 Marks)

ii) 
$$1 + 2t - 3e^{-t} + \frac{1}{3}t^4$$
 (2 Marks)

(2 marks)

c) Let f(x) be function with a period of  $2\pi$  over the interval  $0 < x < 2\pi$  and has period  $2\pi$   $f(x) = \frac{x}{2}$ 

i) Sketch a graph of 
$$f(x)$$
 in the interval  $-2\pi < x < 2\pi$  (4 marks)

- ii) Find the full Fourier representation of the above function (8 marks)
- d) Verify the final value theorem for the function  $3t^2e^{-4t}$  and determine its steady state value.

(3 Marks)

e) Find the Laplace inverse of the following  $L^{-1}\left\{\frac{6}{s^3}\right\}$  (2 marks)

#### **QUESTION TWO**

a) Find the Laplace inverse of the below function by using its partial fractions

$$L^{-1}\left\{\frac{5s^2 + 8s - 1}{(s+3)(s^2 + 1)}\right\}$$
 (9 marks)

- b) Verify the initial value theorem for the voltage function (5 + 2 cos 3t) volts, and state its initial value (4 Marks)
- c) Find the Laplace transform of the following:

i) 
$$L\{e^{-2t}\sin 3t\}$$
 (3 marks)

ii) 
$$L \{2te^{3t} (4\cos 2t - 5\sin 2t)\}$$
 (4 marks)

#### **QUESTION THREE**

Let f(x) = x, be a function of a period  $2\pi$  such that f(x) = x, in the range  $-\pi < x < \pi$ 

- i) Sketch a graph of the above function in the interval  $-3\pi < x < 3\pi$  (4 marks)
- ii) Find the Fourier half sine and cosine series for the above function (12 marks)
- iii) Full Fourier series representation of the above function (4 marks)

#### **QUESTION FOUR**

a) Given that  $f(x) = x^2$  has a period of  $2\pi$  over the interval  $-\pi < x < \pi$ . Show that the Fourier series for f(x) in the interval  $-\pi < x < \pi$  is

$$\frac{\pi^2}{3} - 4 \left[ \cos x - \frac{1}{2^2} \cos 2x + \frac{1}{3^2} \cos 3x - \dots \right]$$

(10 marks)

b) Solve the following differential equations using Laplace transforms

i) 
$$\frac{dx}{dt} - 2x = 4 \text{ at } t = 0, x = 1$$
 (5 Marks)

ii) 
$$\frac{dx}{dt} + 2x = 10e^{3t}$$
 at  $t = 0$ ,  $x = 6$  (5 Marks)