



**MASINDE MULIRO UNIVERSITY OF  
SCIENCE AND TECHNOLOGY  
(MMUST)**

**MAIN CAMPUS**

**UNIVERSITY SPECIAL/SUPPLEMENTARY EXAMINATIONS  
2021/2022 ACADEMIC YEAR**

**THIRD YEAR SECOND SEMESTER EXAMINATIONS**

**FOR THE DEGREE  
OF:**

**BACHELOR OF SCIENCE IN CIVIL AND STRUCTURAL  
ENGINEERING**

**BACHELOR OF TECHNOLOGY IN BUILDING CONSTRUCTION**

**COURSE CODE: CSE 312**

**COURSE TITLE: PLASTIC ANALYSIS OF STRUCTURES**

**DATE: 01<sup>ST</sup> AUGUST 2022      TIME: 8:00AM – 10:00AM**

**INSTRUCTIONS:**

1. This paper contains **FIVE** questions
2. Answer **QUESTION ONE** and any other **TWO** Questions
3. Marks for each question are indicated in the parenthesis.
4. Examination duration is **2 Hours**

MMUST observes **ZERO** tolerance to examination cheating

This Paper Consists of 4 Printed Pages. Please Turn Over.

**QUESTION ONE (30 MARKS)**

- a) Define the following terms as used in plastic analysis of structures. **(5mks)**
- (i) Plastic design
  - (ii) Plastification
  - (iii) Plastic hinge
  - (iv) Shape factor
  - (v) Plastic moment
- b) State any THREE fundamental differences between elastic analysis and plastic analysis of structures. **(6mks)**
- c) A steel beam shown in Figure Q1 is to be used in the construction of a bridge of length,  $L = 4\text{m}$ .
- (i) Determine the shape factor of the structure. **(4mks)**
  - (ii) Explain the significance of the factor calculated in (i) above. **(2mks)**
  - (iii) Calculate the collapse load using the kinematic method of plastic analysis. (Assume that the plastic moment is constant throughout the beam, and the yield stress is 500MPa). **(13mks)**

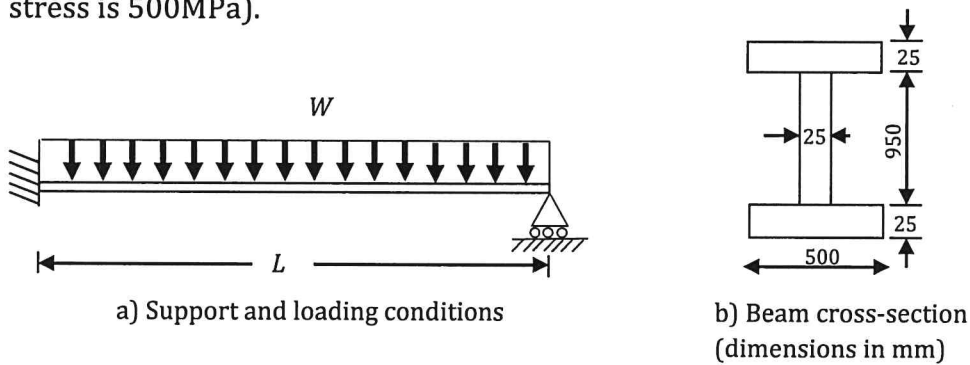


Figure Q1

**QUESTION TWO (20 Marks)**

- a) Postulate the collapse mechanisms of the structures under the influence of monotonically increasing static load configurations given in Figure Q2(a). **(4mks)**

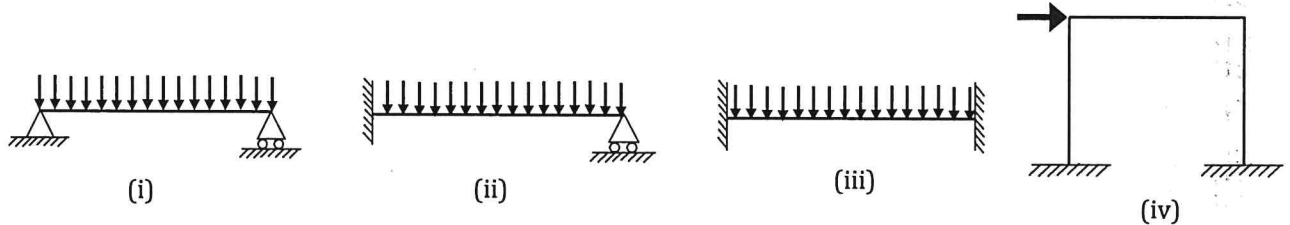


Figure Q2(a)

- b) Evaluate using virtual work method, the ultimate load,  $W_c$ , required to cause collapse of a beam loaded as shown in Figure Q2(b). The material making the beam has plastic moment,  $M_p = 100 \text{ kNm}$ . **(16mks)**

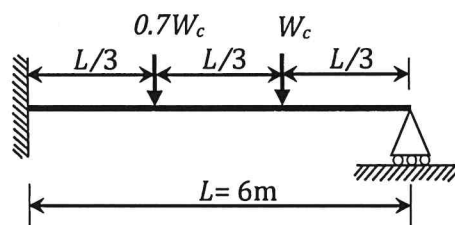


Figure Q2(b)

### QUESTION THREE (20 Marks)

- a) State and explain the THREE theorems of plastic collapse. **(6mks)**  
 b) Postulate the yield line pattern for the slab configurations shown in Figure Q3. **(6mks)**

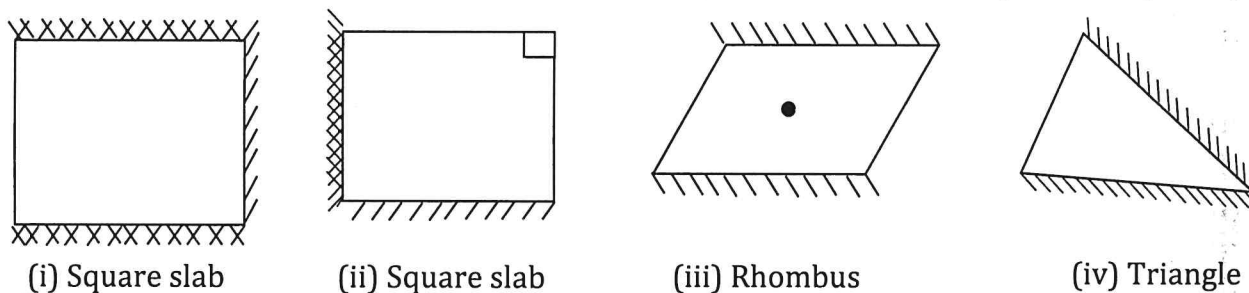


Figure Q3

- c) Evaluate the ultimate load for a square concrete slab which is simply supported on all four edges, isotropically reinforced, side length  $L$  and moment of resistance  $m$  per unit length. **(8mks)**

### QUESTION FOUR (20 Marks)

- a) Differentiate between plastic hinge and mechanical hinge. **(4mks)**  
 b) An isotropically reinforced rectangular slab is simply supported along all four sides and subjected to a uniformly distributed load of  $w$  kN/m<sup>2</sup> as shown in Figure Q4. Show that the ultimate load that the slab can carry using mechanism method of plastic analysis is given by: **(16mks)**

$$W_u = \frac{24m}{\alpha^2 L^2} \left( \frac{1}{\sqrt{3 + \mu\alpha^2} - \alpha\sqrt{\mu}} \right)^2$$

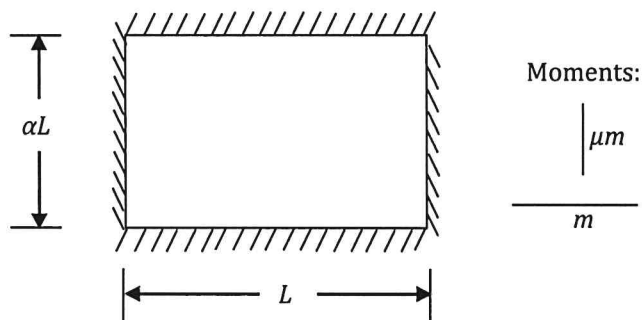


Figure Q4

### QUESTION FIVE (20 Marks)

A rigid-jointed frame with the relative  $M_p$  values and the applied collapse load is as shown in Figure Q5. Determine the required  $M_p$  value, the value of the support reactions and sketch the bending moment diagram at collapse. **(20mks)**

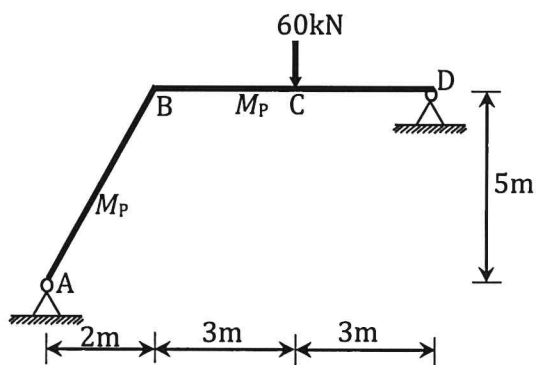


Figure Q5

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