



*(University of Choice)*

**MASINDE MULIRO UNIVERSITY OF  
SCIENCE AND TECHNOLOGY  
(MMUST)**

**UNIVERSITY EXAMINATIONS  
2021/2022 ACADEMIC YEAR**

**THIRD YEAR SECOND SEMESTER MAIN EXAMINATIONS**

**FOR THE DEGREE  
OF  
BACHELOR OF SCIENCE IN PHYSICS**

**COURSE CODE: SPH 355**

**COURSE TITLE: WIND ENERGY SYSTEMS**

**DATE: FRIDAY 29<sup>TH</sup> APRIL, 2022      TIME: 12:00 PM - 2:00 PM**

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**INSTRUCTIONS TO CANDIDATES**

**Answer QUESTION ONE and any TWO QUESTIONS .**

**Symbols used bear the usual meanings.**

**YOU MAY USE THE FOLLOWING CONSTANTS**

Density of air =  $1.225 \text{ kg/m}^3$

MMUST observes ZERO tolerance to examination cheating

This Paper Consists of 3 Printed Pages. Please Turn Over.

**QUESTION ONE (30 marks)**

- a) Define the following terms as used in wind turbine systems
- i. Solidity
  - ii. Tip speed ratio (2 marks)
- b) Discuss social, economic and environmental impact of wind energy (3 marks)
- c) Distinguish between a wind turbine and a wind mill (1 mark)
- d) A rotor diameter of two bladed HAWT is 6.5m. At its rated wind speed of 10 m/s, the power output of the turbine is 15 kW.
- i. Find the efficiency of the turbine at this wind speed (2 marks)
  - ii. Calculate the tip speed ratio if the blades are rotating at 230 rpm (2 marks)
- e) Show that the air speed through actuator disc (turbine) is the average of the upstream and downstream wind speed (3 marks)
- f) By differentiating the expression for power coefficient  $C_p = 4a(1-a)^2$ , with respect to  $a$  (axial induction factor or axial interference factor), show that the maximum value of  $C_p$  is  $16/27$  when  $a = 1/3$ . (3 marks)
- g) Enumerate any three benefits of offshore wind farms compared with onshore wind farms. (3 marks)
- h) Discuss losses associated with small wind turbines (3 marks)
- i) Sketch wind aerodynamics for stationary airfoil and airfoil in motion. Indicate all the forces acting on the airfoil. (4 marks)
- j) In terms of yaw operations, explain the design considerations for two rotor blade design and three rotor blade design. (2 marks)
- k) Explain any two advantages of VAWTs (2 marks)

**QUESTION TWO (20 MARKS)**

- a) A wind turbine with a rotor diameter of 56 m is rated at 1 MW at a hub height wind speed of 12 m/s. It has a cut-in speed of 3.5 m/s and a cut-out speed of 24 m/s. Assume that this machine is located at a site where the mean wind speed is 10 m/s and that a Rayleigh wind speed distribution can be used. Calculate the following:
- (i) The number of hours per year that the wind is below the cut-in speed. (4 marks)
  - (ii) The number of hours per year that the machine will be shut down due to wind speeds above the cut-out velocity. (4 marks)
- b) Using well labelled diagrams describe the power curve parameters (5 marks)
- c) Discuss the various models employed in describing wind flow. (4 marks)
- d) Explain the various sources of uncertainties that impede accurate assessment of wind flow. (3 marks)

**QUESTION THREE (20 MARKS)**

- a) Show that the power content of a cylindrical column of air is proportional to the square of its diameter  $D$  and cube of its speed  $V$ . (4 marks)
- b) Explain the advantages and disadvantages of three-bladed rotor over two bladed rotor (3 marks)

- c) Discuss three planning constraints that make it difficult to install a wind turbine in any farm. (3 marks)
- d) Describe stages of development before a wind turbine/ farm can be approved and built. (10 marks)

#### QUESTION FOUR (20 MARKS)

- a) Using suitable illustrations, discuss how mechanical wind mills are used in water pumping (5 marks)
- b) Deduce the relation between performance coefficient, torque coefficient and tip speed ratio for a system of turbines. (4 marks)
- c) Discuss the design principle of horizontal axis wind turbines (HAWTs) and vertical axis wind turbines (VAWTs) (4 marks)
- d) A 35 m diameter three bladed wind turbine produces 720 kW at a wind speed of 12 m/s. Find:
- The rotational speed (rpm) of the rotor at a tip speed ratio of 4 (2 marks)
  - What is the tip speed in m/s (1 mark)
  - If the generator turns at 1700 rpm. What gear ratio is needed to match the rotor speed to the generator speed? (2 marks)
  - The efficiency of the wind turbine system (including blades, transmission, shafts and generator) under these conditions? Assume Betz limit  $C_p = 16/27$  (2 marks)

#### QUESTION FIVE (20 marks)

- a) State policy options available for wind turbines (4 marks)
- b) State any three factors that have accelerated the wind power technology development. (3 marks)
- c) Explain two sets of factors in which the amount of wind energy available at any locations depends on. (2 marks)
- d) Give the similarities and differences between Rayleigh and Weibull distribution (3 marks)
- e) Analysis of time series data for a given site has yielded an average velocity of 5 m/s. It is determined that a Rayleigh wind speed distribution gives a good fit to the wind data.
- Based on a Rayleigh wind speed distribution, estimate the number of hours that the wind speed will be between 9.0 and 10.0 m/s during the year. (4 marks)
  - Using a Rayleigh wind speed distribution, estimate the number of hours per year that the wind speed is equal to or above 15 m/s. (4 marks)