



(University of Choice)

**MASINDE MULIRO UNIVERSITY OF  
SCIENCE AND TECHNOLOGY  
(MMUST)**

**MAIN CAMPUS**

**SPECIAL/SUPPEXAMINATIONS  
2021/2022 ACADEMIC YEAR**

**SECOND YEAR SECOND SEMESTER EXAMINATIONS**

**FOR THE AWARD  
OF  
DIPLOMA IN ENGINEERING**

**COURSE CODE: DEE 082**

**COURSE TITLE: CONTROL SYSTEMS**

**DATE: Thursday 6<sup>th</sup> Oct, 2022**

**TIME: 8.00a.m – 10.00A.m**

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**INSTRUCTIONS TO CANDIDATES**

ANSWER QUESTION ONE AND ANY OTHER TWO QUESTIONS.  
QUESTION ONE CARRIES 30 MARKS AND ALL OTHERS 20 MARKS EACH.

TIME: 2 Hours

MMUST observes ZERO tolerance to examination cheating

This Paper Consists of 4 Printed Pages. Please Turn Over. 

## Question One

- a. Define the following terms as applied in control engineering;
- i. Self loop [1 mark]
  - ii. Path [1 mark]
  - iii. Sink [1 mark]
  - iv. Node [1 mark]
  - v. Locus [1 mark]
  - vi. Loop gain [1 mark]

- b. Develop the Nyquist path for the Type 0 continuous system below. [5 marks]

$$GH = \frac{1}{(s + 1)}$$

- c. Devise a control system to fill a container with water after it is emptied through a stopcock at the bottom. The system must automatically shut off the water when the container is filled. Use clearly labeled diagram. [2 marks]
- d. Construct a signal flow graph for the simple resistance network given in Figure 1d below and find its transfer function using the gain formula. [6 marks]

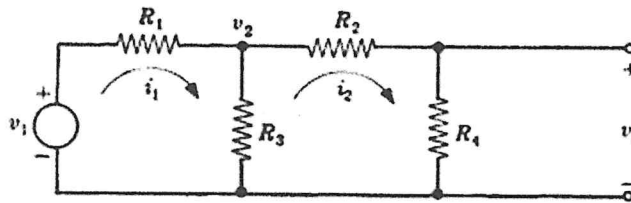


Figure 1d

- e. Determine the angle and magnitude of  $GH(j2)$  for  $GH = k/s(s+2)^2$  hence find the value of  $k$  that satisfies  $|GH(j2)| = 1$  [5 marks]
- f. Give any *six* properties of mapping of  $P(s)$  to  $P(z)$ . [6 marks]

## Question Two

- a. Determine;
- i. The condition under which the Bode magnitude plot for a pair of complex poles has a break at a nonzero, finite value of  $\omega$  [5 marks]
  - ii. The frequency at which the peak value occurs [3 marks]

- b. Find the angles and centre of, and sketch the asymptotes of [6 marks]

$$GH = \frac{k(s + 2)}{(s + 1)(s + 3 + j)(s + 3 - j)(s + 4)}$$

- c. Find the breakaway point between 0 and -1 for [3 marks]

$$GH = \frac{k}{s(s + 1)(s + 3)(s + 4)}$$

- d. Determine the Bode form and Bode gain for the transfer function [3 marks]

$$GH = \frac{k(s+2)}{s^2(s+4)(s+6)}$$

### Question Three

- a. Outline the *four* properties of polar plots. [4 marks]
- b. Consider the Figure 3b below; find the position, velocity, and acceleration error constants. [6 marks]

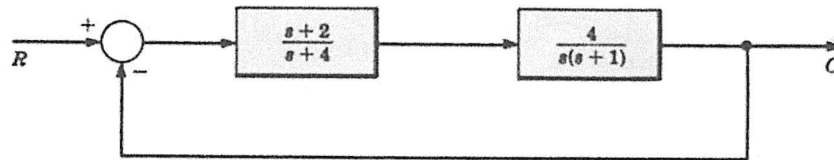
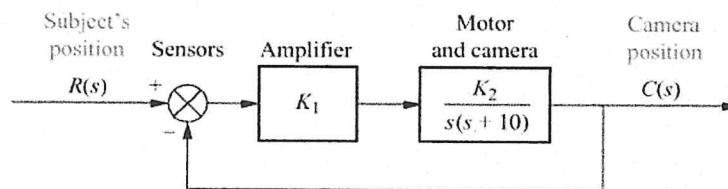


Figure 3b

- c. Determine if the following characteristic equation represents a stable system using the Routh stability criterion  $S^3 + 4S^2 + 8S + 12 = 0$ . [3 marks]
- d. Consider the continuous system in Figure below. The design value for the gain factor is  $K$ , plot a sketch of the root locus.



[7 marks]

### Question Four

- a. With the aid of appropriate sketches and equations give any *three* singularity functions used in control systems. [3 marks]
- b. Determine the damping ratio  $\zeta$ , undamped natural frequency  $\omega_n$ , damping coefficient  $\alpha$ , damped natural frequency  $\omega_d$ , and time constant  $\tau$  for the following second-order control system; [4 marks]

$$\frac{d^2y}{dt^2} + 5\frac{dy}{dt} + 9y = 9u$$

- c. Compare the proportional, integral and differential controllers. [3 marks]
- d. Construct the polar plot of the Type 1 digital control system with open loop transfer function. [10 marks]

$$GH = \frac{k/4}{(z-1)\left(z-\frac{1}{2}\right)}$$

### Question Five

- a. Determine the transfer function of the system plotted in the figure 5a below if it has a gain of 9. [4 marks]

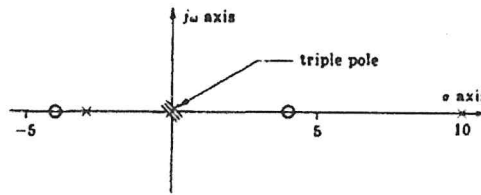


Figure 5a

- b. Show that the dB magnitude-phase angle for a pole of order  $l$  at the origin of the s-plane  $1/(j\omega)^l$  is a straight line parallel to the dB magnitude axis with an abscissa of  $-90l^\circ$  for  $\omega \geq 0$ . [6 marks]
- c. Construct a sketch of the dB magnitude-phase angle plot for the continuous time open loop transfer function [10 marks]

$$GH = \frac{2}{s(1+s)(1+s/3)}$$