



(University of Choice)

**MASINDE MULIRO UNIVERSITY OF
SCIENCE AND TECHNOLOGY
(MMUST)**

MAIN CAMPUS

**UNIVERSITY EXAMINATIONS
2023/2024 ACADEMIC YEAR**

FIFTH YEAR FIRST SEMESTER EXAMINATIONS

**FOR THE DEGREE
OF
BACHELOR OF SCIENCE IN ELECTRICAL AND
COMMUNICATION ENGINEERING**

COURSE CODE: ECE 511E

COURSE TITLE: POWER SYTSEM ANALYSIS

DATE: THURSDAY 07/12/2023 TIME: 3: 00 PM – 5:00 PM

INSTRUCTIONS TO CANDIDATES

ANSWER QUESTION ONE AND ANY OTHER TWO QUESTIONS.
QUESTION ONE CARRIES 30 MARKS AND ALL OTHERS 20 MARKS EACH.

TIME: 2 Hours

MMUST observes ZERO tolerance to examination cheating

This Paper Consists of 4 Printed Pages. Please Turn Over. 

Question 1 (30 Marks)

- (a) Explain under what circumstances we can use small signal analysis in analyzing power system stability and a technique that is used therein. (5 marks)
- (b) A 6000 bus system has 900 generators, all of which are modeled in a power flow program with specified terminal voltage and reactive limits, i.e., they are voltage-controlled buses, and there are no other voltage-controlled buses besides these 900 generator buses. At the beginning of the Newton Raphson solution procedure (initialization of iteration 1), answer the following:
- i How many type PV buses are there in the power flow model?. (1 mark)
 - ii How many type PQ buses are there in the power flow model?. (1 mark)
 - iii How many bus voltage magnitudes are unknown? (1 mark)
 - iv How many bus voltage angles are unknown? (1 marks)
 - v What is the number of power flow equations used? (2 marks)
- (c) Use Gauss-Seidel method to find the solution to the following equations, use initial estimates $x_1^{(0)} = 1, x_2^{(0)} = 2$, perform 2 (two) iterations (4 marks)

$$x_1 + x_1x_2 = 10$$

$$x_1 + x_2 = 6$$

- (d) A 50-Hz synchronous generator has a transient reactance of 0.2 per unit. The generator is connected to an infinite bus through a transformer and a double circuit transmission line, as shown in Figure 1. Resistances are neglected and reactances are expressed on a common MVA base and are marked on the diagram. The generator is delivering a real power of $P_e = 0.77$ per unit to bus bar 1. Voltage magnitude at bus 1 is 1.1. The infinite bus voltage $V = 1.0\angle 0^\circ$ per unit. Determine
- (a) power angle δ_1 in degrees (2 marks)
 - (b) current, I flowing between buses 1 and 2 in rectangular form. (2 marks)
 - (c) The excitation voltage of the generator, E' in polar form. (2 marks)

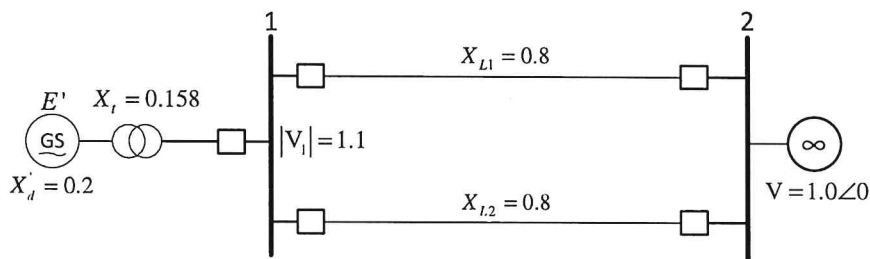


Figure 1: Single Machine Infinite bus

- (e) A single area consists of two generating units, rated at 400 and 800 MVA, with speed regulation of $R_1 = 4\%$ percent and $R_2 = 5\%$ on their respective ratings. The units are operating in parallel, sharing 700 MW. Unit 1 supplies 200 MW and unit 2 supplies 500 MW at 1.0 per unit (50 Hz) frequency. The load is increased by 130 MW.
- Express the governor speed regulation of each unit and the load change to a common 1000 MVA base. (2 marks)
 - the per unit steady-state frequency deviation. (2 marks)
 - the new system frequency. (2 marks)
 - the change in generation for each unit in MW (3 marks)

Question 2 (20 Marks)

- Write the power flow equations in polar form for buses $i = 1, 2, \dots, n$; and explain why they cannot be solved using direct methods. (4 marks)
- The power-angle relationship for the network of Fig. 2 is given as $P_e = \frac{V_g V_b}{X} \sin \delta = 2.087 \sin \delta$. A short circuit occurs in the middle of the line L_2
 - draw the equivalent circuit indicating the reactances during the short circuit. (3 marks)
 - determine the power-angle relationship during the short circuit in the middle of the line. (4 marks).
 - Determine the power-angle relationship after the fault is cleared by outage of line L_2 (4 marks)

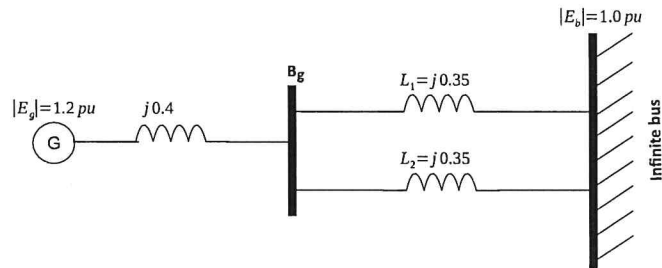


Figure 2: Single machine infinite bus system

- Define a *voltage controlled bus* as used in a power flow study and explain what quantity is allowed to change in such a bus during computations and in what manner. (4 marks)

Question 3 (20 Marks)

- (a) A set of linear algebraic equations representing a power system in matrix format is given as $\mathbf{Ax}=\mathbf{y}$, the determinant $\det(\mathbf{A})$ is found to be negative. Will such a system of equations converge when performing load flow? Briefly explain. (4 marks)
- (b) In the two-bus system shown in Fig. 3, bus 1 is a slack bus with $V_1 = 1.0\angle 0^\circ$. A load of 100 MW and 50 MVAR is taken from bus 2. The line impedance is as indicated on a base of 100 MVA. Initial estimate of $V_2^{(0)} = 1.0$ p.u. and $\delta_2^{(0)} = 0^\circ$.
- Express the load in per unit. (1 mark)
 - Determine Y_{bus} in polar form. (1 mark)
 - Write the power flow equations for P and Q in polar form (use the admittance values obtained in (ii) above). (2 marks)
 - Determine the Jacobian elements of (iii) above. (4 marks)

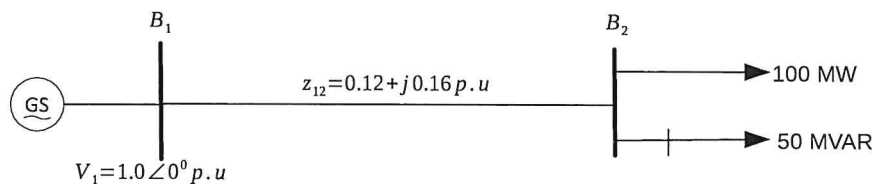


Figure 3: Single line diagram of two bus system

- (c) Briefly explain why generator frequency rather than electric torque T_e or electrical power P_e is used as a control signal to indicate/detect power imbalance in a power system. (4 marks)
- (d) Explain critical clearing time and critical clearing angle. (4 marks)

Question 4

- (a) Explain principle underlying the approach of the fast-decoupled load flow (FDLF), use appropriate Jacobian matrix elements in your explanation. (8 marks)
- (b) In terms of critical clearing angle δ_{cc} , briefly explain the importance of critical clearing time, t_{cc} on transient stability. (5 marks)
- (c) A generator delivers power of 1.0 p.u. to an infinite bus through a purely reactive network. The maximum power that could be delivered by the generator is 2.0 p.u. A three-phase fault occurs at the terminals of the generator which reduces the generator output to zero. The fault is cleared after time, t_c second. The original network is then restored. The maximum swing of the rotor angle is found to be $\delta_{max} = 110^\circ$ electrical degree. Find the rotor angle in electrical degrees at $t = t_c$. (7 marks)

Question 5

- (a) Derive the swing equation as used in power system stability studies, and state what class of stability studies it is used for. (8 marks)
- (b) A 50 Hz interconnected power system has two areas denoted area 1 and area 2, where the area frequency response characteristics are given by $\beta_1 = 100$ MW/Hz and $\beta_2 = 100$ MW/Hz. The total power generated in each of these areas is 500 and 250 MW, respectively. Each area is initially generating power in steady state with $\Delta P_{tie1} = \Delta P_{tie2} = 0$ when the load in area 1 suddenly increases by 60 MW. Compute the resulting steady state change in frequency Δf as well as the steady state changes in tie-line flows ΔP_{tie1} and ΔP_{tie2} with Load frequency control (LFC). (8 marks)
- (c) Briefly describe what is meant by the transient state of a power system, and when a power system is said to be transiently stable. (4 marks)

