

Question One (Compulsory) (25 MARKS)

- a. Differentiate between the following terms. (6 marks)
- A n estimate and an estimator
 - Linear and non linear correlation
 - Relative risk and odds ratio

b. Study the table below hence attempt the following questions;

Habitat	Death by suicide	
	Yes	No
Inner city	102	59898
Surburbs	121	189879

- Obtain the relative risk. (4 marks)
 - Compute the 95% CI for the relative risk. Interpret your results. (5 marks)
- c. Outline the procedure for downloading optional packages in R. (10 marks)

Question Two (25 MARKS)

a.

$$P = \begin{bmatrix} 2 & 7 & 4 \\ 6 & 1 & 3 \\ 8 & 4 & 5 \end{bmatrix} \quad \text{and} \quad Q = \begin{bmatrix} 6 & 7 & 1 \\ 2 & 9 & 2 \\ 3 & 3 & 5 \end{bmatrix}$$

Using the three matrices in (a) above, write a code to perform the following:

- Determines PQ(1 marks)
- Determines P+Q(1 marks)
- Calculates the determinant of P (1 marks)
- Computes the inverse of PQ (1 marks)
- Augments matrix P to Q column wise (1 marks)
- Evaluates $P^2+2P+P/Q+3$ (2 marks)

b. Consider the following data called *ExamData* which we assume to be saved as a text file in a folder called *StatisticalData* in the C directory.

Weight	51	59	64	76	93	106	125	149	171	199
age	2	4	6	8	10	12	14	16	18	20

Write a single well commented program in R that does the following:

- Reads the above data into R (2 marks)
- Sorts the weights into decreasing order (1 marks)
- Computes the minimum and the maximum values of both weight and age. (4 marks)
- Plots the scatter diagram of weight against age where; (7 marks)
 X-axis is labeled as 'Age'
 Y-axis is labeled as 'Weight'

The main title of the graph is 'A graph of weight against age'
 The sub title is 'Question one graph'

- (v). Superimpose a straight line of best fit to the graph in (iv) above. (2 marks)
 (vi). Summarize each of the above variables Weight and Age in a histogram (2 marks)

Question Three (25 MARKS)

The data below shows the household expenditure, income and savings. Fit the least squares regression model to determine the amount of expenditure given that income is \$10 and savings is \$2.

Income	12	15	8	5
Savings	3	1	0	2
expenditure	4	3	2	1

(25 marks)

Question Four (25 MARKS)

- a. Define the term discriminant analysis and hence state the underlying assumptions in studying it. (5 marks)
 b. Given that $\bar{X}_1 = (20 \ 2 \ 12)^T$ comes from population 1 and $\bar{X}_2 = (17 \ 9 \ 2)^T$ comes from population 2 and both populations have a common covariance matrix,

$$S = \begin{pmatrix} 20 & -4 & 15 \\ -4 & 16 & 0 \\ 15 & 0 & 4 \end{pmatrix}$$

Use discriminant analysis to classify $X = (24 \ 1 \ 3)$ (20 marks)

Question Five (25 MARKS)

- a. Consider two samples of data X and Y such that $n_1 = n_2 = 9$.

$$\bar{X} = 35.22, \sum X^2 = 11361, \bar{Y} = 31.56, \sum Y^2 = 9122$$

Estimate the true mean difference $\mu_1 = \mu_2$ at 5% level of significance. (15 marks)

- b. The following results were obtained in a study to identify whether disease was associated with exposure to non-treated water

Untreated water	case	control
Yes	55	19
No	128	164

- i. Calculate the odds ratio and discuss your results (4 marks)
- ii. Calculate the 95% confidence interval for the OR. Interpret your results. (6 marks)